Heavy Neutral Lepton on Future Muon Collider

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Outline

- Neutrino Mass
- Heavy Neutral Leptons
- Search at Future Muon Collider
 - Muon flavor
- Various Experimental Constraints

Origin of Neutrino Mass

- In SM, neutrino is massless. While the experiments have confirmed its tiny mass smaller than O(0.1) eV.
- Effective Operator: Weinberg Operator $\frac{LLHH}{\Lambda}$
- Seesaw mechanism
 - Simple Type I
 - Inverse seesaw model
 - Linear seesaw model
- We choose to work in a simple scenario. Suppose there is heavy neutral lepton. We can parametrize its mass m_N mixing angle with SM neutrino. $U_l = \sin \theta_l$

$$\mathcal{L}_{W} = \frac{gU_{l}}{\sqrt{2}} \left(W_{\mu} \bar{l}_{L} \gamma^{\mu} N + h.c. \right)$$

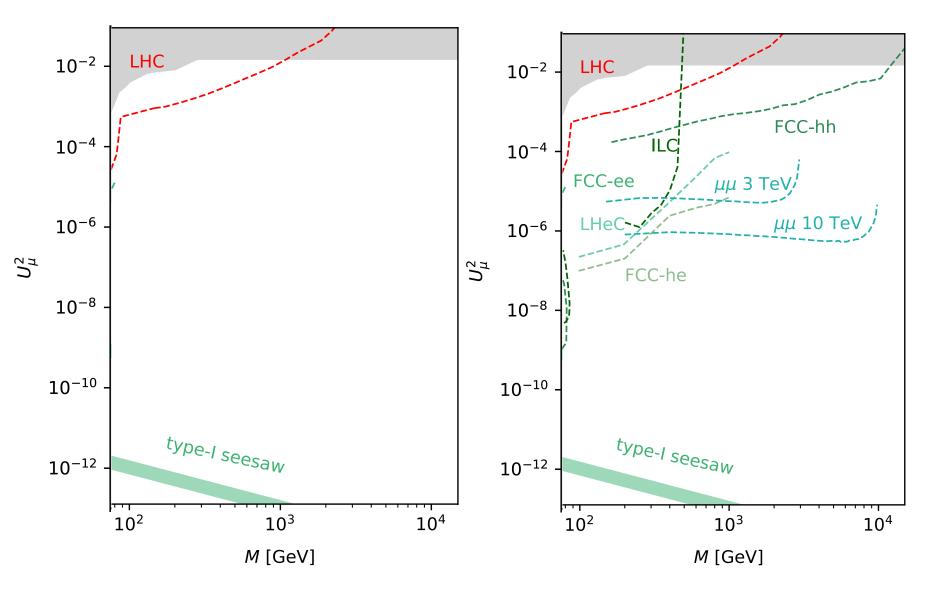
$$\mathcal{L}_{Z} = -\frac{gU_{l}}{2 \cos \theta_{w}} Z_{\mu} \left(\bar{\nu}_{L} \gamma^{\mu} N + \bar{N} \gamma^{\mu} \bar{\nu}_{L} \right)$$

$$\mathcal{L}_{H} = -\frac{U_{l} m_{N}}{2} h \left(\bar{\nu}_{L} N + \bar{N} \nu_{L} \right)$$

 $\mathcal{L} = \mathcal{L}_W + \mathcal{L}_Z + \mathcal{L}_H$

Our current focus

$$m_N > O(100) \text{GeV}$$



The muon collider can open and probe new region space in the parameter space. even compared to other future colliders!

Snowmass Energy Frontier Report: 2211.11084

Search at Muon Collider

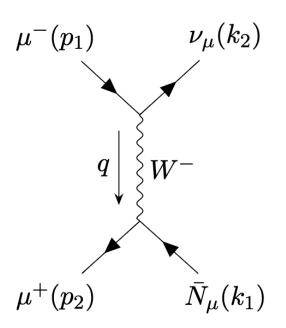
- The future muon collider includes 3 TeV and 10 TeV scenarios.
- Clean background, fixed cms energy, excellent environment for the muon flavor HNL
- Here we show the muon-flavor Dirac HNL as benchmark.

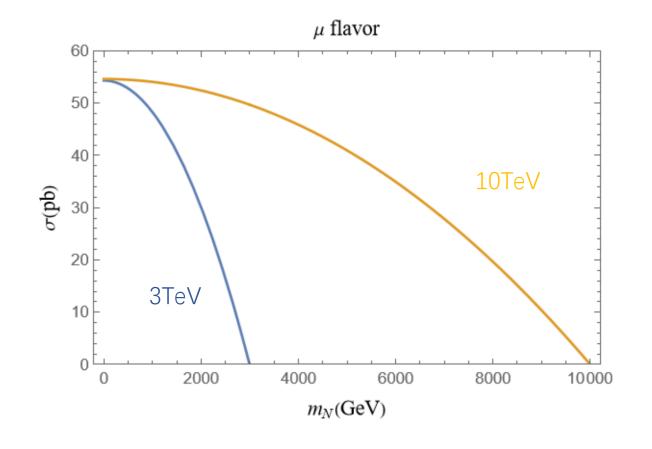
- Tools:
 - Using MadGraph 3.4 to simulate and then make analysis
- Effective Vector-Boson Approximation (EVA) or gauge boson PDF has been implemented

Muon Flavor

 ${}^{\bullet}$ Signal: Production of N_{μ} Dominated by the t-channel

$$\mu^{+} + \mu^{-} \to N_{\mu} + \bar{\nu}_{\mu}$$





Type	Signal process	$\sigma/U_{\mu}^2(m_N = 1000 \text{GeV})$
t-channel	$\mu^+\mu^- \longrightarrow N_\mu \bar{\nu}_\mu$	48.26 pb
VBF	$\mu^{+}\mu^{-} \longrightarrow \mu^{+}\mu^{-}N_{\mu}\bar{\nu}_{\mu}$	$\sim 1~\mathrm{pb}$
VBF	$\mu^+\mu^- \longrightarrow \bar{\nu}_{\mu}\nu_{\mu}N_{\mu}\bar{\nu}_{\mu}$	$\sim 0.1~\mathrm{pb}$

Table 1: Signal for μ flavor at 3 TeV

Decay of N_{μ}

HNL can promptly decay via neutral current or charged current or to the higgs. Here we select its decay channel to W boson.

$$N_{\mu} \to W^{+} + \mu^{-}, W^{+} \to jj$$

We assume the W boson can be well reconstructed from the two jets.

We focus on the final states W^+ and μ^- and reconstruct its invariant mass distribution.

10TeV Background

Dijets can be from either W or Z boson.

Type	Background process	σ/U_{μ}^2	Cut	Taking account
t-channel	$\mu^+\mu^- \longrightarrow W^+\mu^-\bar{\nu}_{\mu}$	0.107 pb	default cut	Yes
t-channel	$\mu^+\mu^- \longrightarrow Z\mu^+\mu^-$	$0.232~\mathrm{pb}$	default cuts & missing μ^+	Yes
VBF	$\mu^+\mu^- \longrightarrow \mu^+\mu^-W^+\mu^-\bar{\nu}_{\mu}$	$0.2~\mathrm{pb}$	default cut $(\mu^+\mu^-)$ are missing)	Yes
VBF	$\mu^+\mu^- \longrightarrow \bar{\nu}_{\mu}\nu_{\mu}W^+\mu^-\bar{\nu}_{\mu}$	0.0343 pb	$\operatorname{default}\operatorname{cut}$	No

TABLE IV. Background for μ flavor at 10 TeV

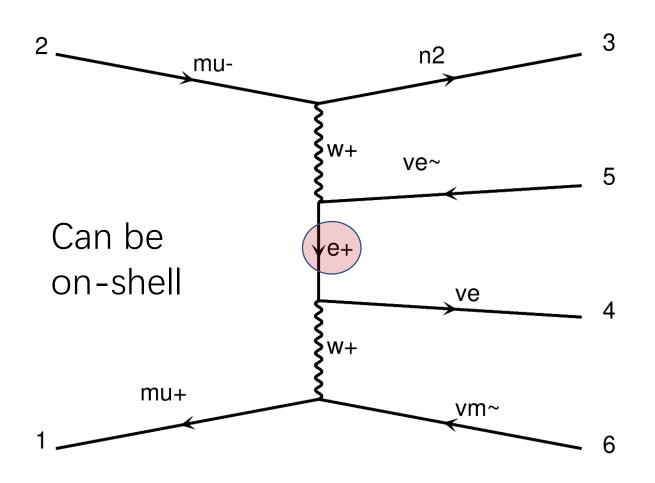
Using EVA in MadGraph, especially photon PDF VBF processes dominates at 10 TeV

Default cut: For muon: PT > 20GeV, Eta < 2.5

Using EVA will lead to t-channel singularity.

So we just generate 2 -> 5 processes directly in MadGraph.

(Real) t-channel singularity

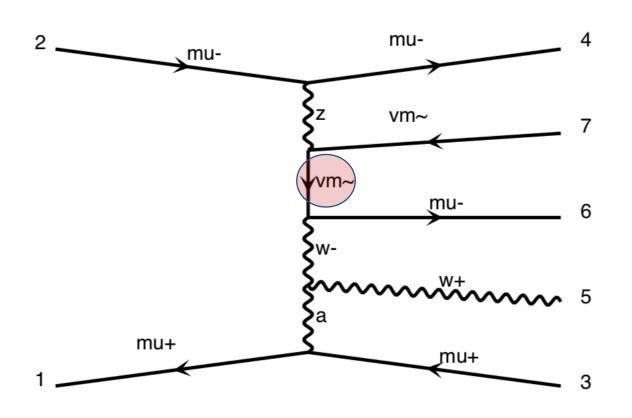


Complex mass regulation hep-ph/9509314

The cross section is proportional to the beam size. hep-ph/9601290

We are trying to gain a better understanding. (In progress)

(Fake) t-channel singularity: Subtlety of EVA



In 2 to 5 full processes, the intermediate neutrino can never be on-shell.

But in EVA, if we treat the gauge boson are "real", the neutrino can be on-shell which induce t-channel singularity.

One plausible way is to make the light particles are from the decay of heavy gauge bosons.

Cutflow Analysis

- 1. We assume the W boson can be well constructed from the dijets (Z boson can fake).
- 2. Combine the $W^+(Z)$ and μ^- to try to reconstruct the HNL

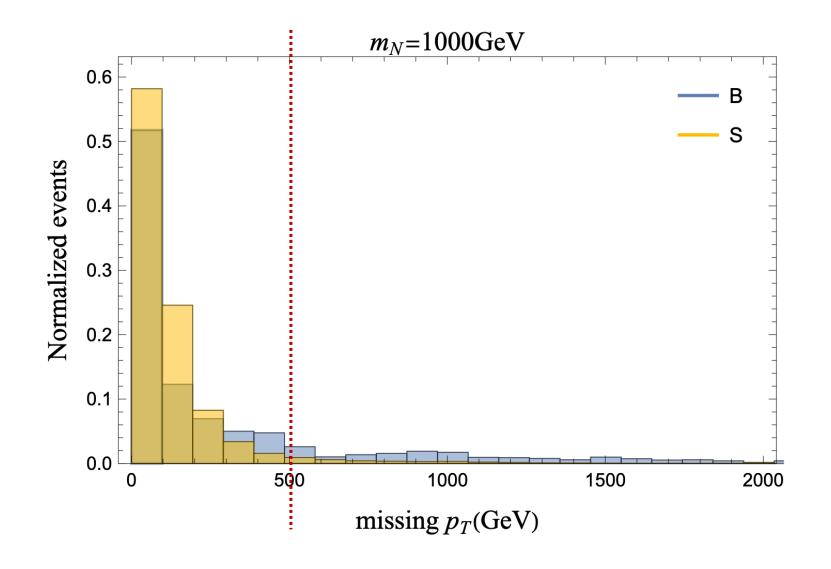
Impose the mass window:

Require a cut around the heavy neutrino mass.

$$m_N < 500 {\rm GeV}: m_N \pm 0.1 m_N$$

$$m_N \ge 500 \text{GeV}: \qquad m_N \pm 50 \text{GeV}$$

After mass window selection

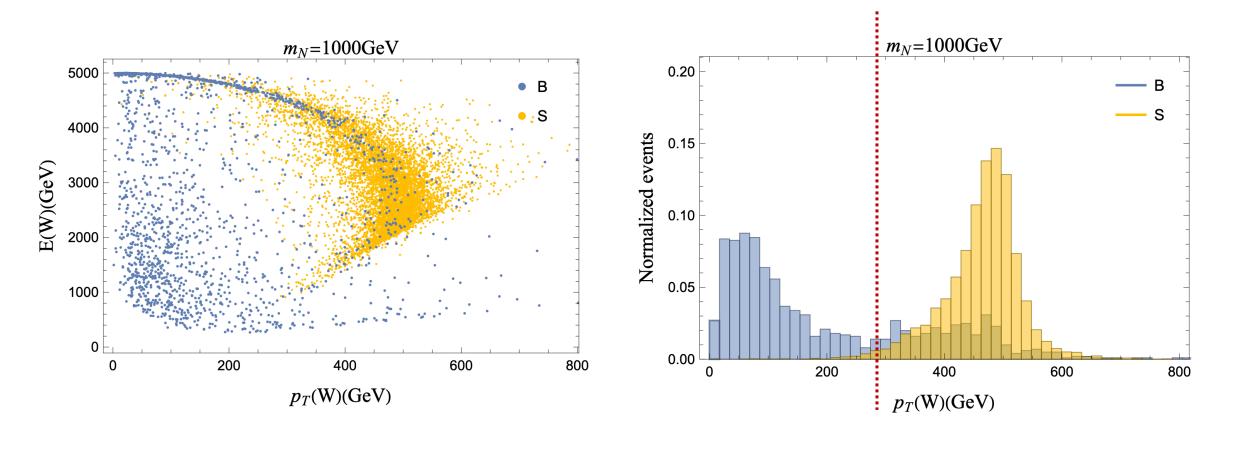


Optimization cuts I:
 Missing transverse
momentum needs to be
less than 500 GeV.

Optimization cuts II:

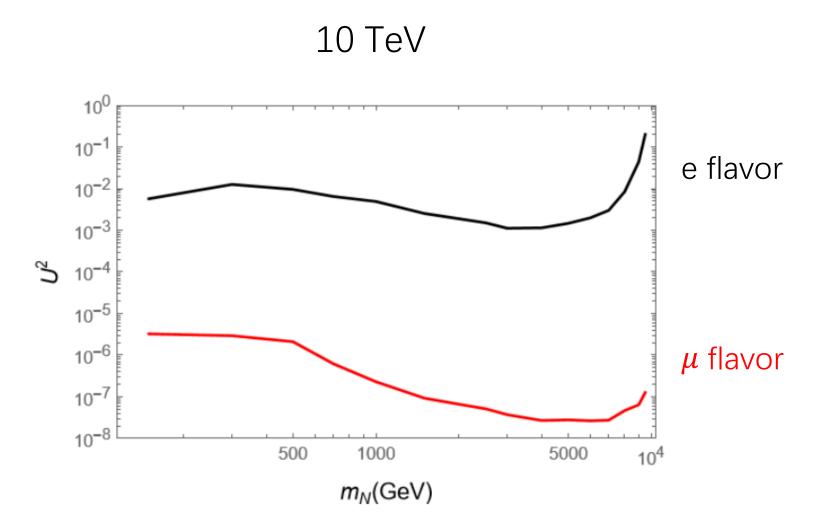
For the reconstructed W boson.

1000GeV<E(W)<4950GeV which is mass window dependent



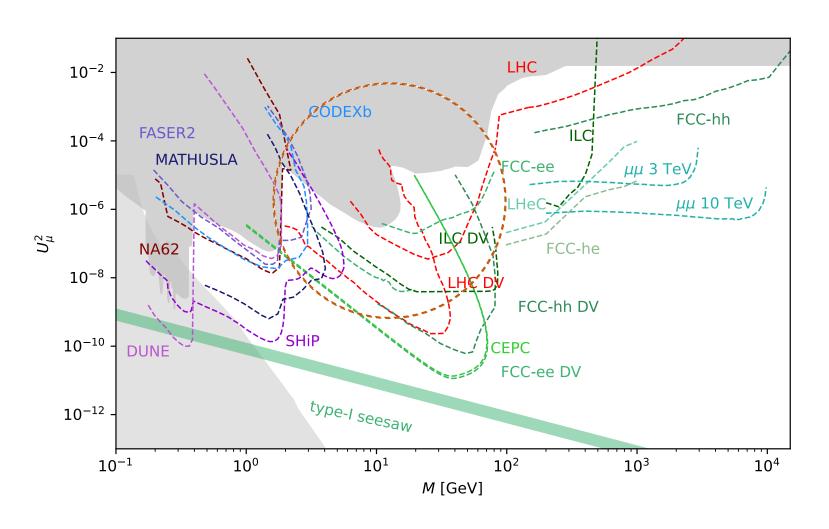
Final Results

95% exclusion bounds



Various Bounds

Next step



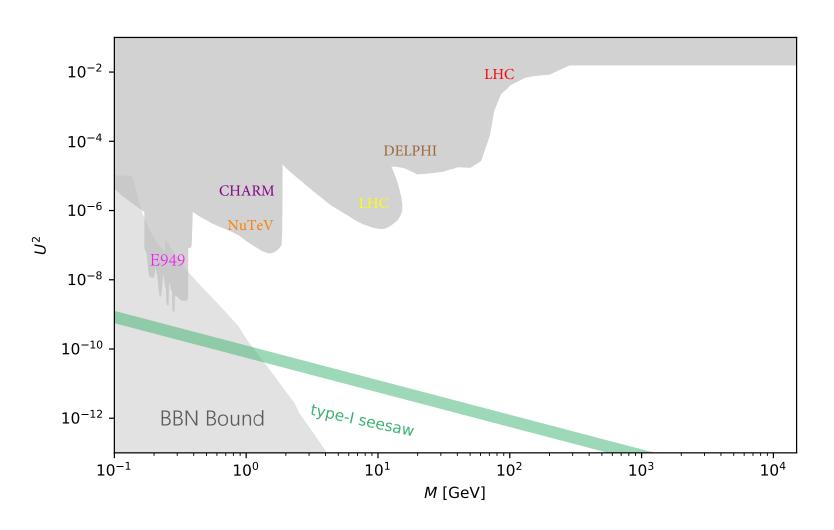
Short Review of Various Probes

- People have tried to constrain in the U^2-mN plane via various channels and different machines.
- Cosmo and astrophysical probe: BBN, CMB, etc
- Indirect constraints: branching ratio of SM particles decays, etc
- Direct constraints
 - Production
 - Meson decay, heavy lepton decay
 - (On-shell/Off-shell) Gauge/higgs boson decay
 - Decay
 - Short-lived
 - Long-lived

Existing Bounds

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From Past Experiments



NuTeV: Drell-Yan, NHL decay

CHARM:

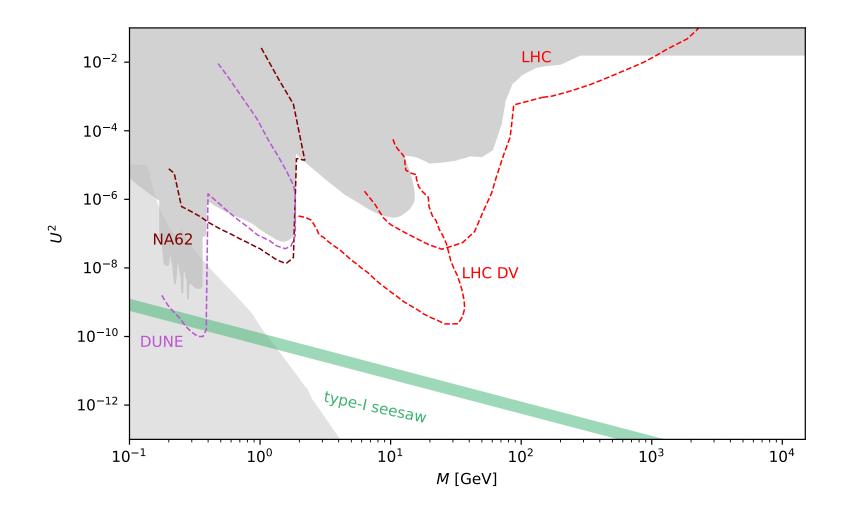
Beam-dump: D meson decay, Wide-band: neutrino beam colliding with nucleus

DELPHI: Z boson decay

E949: Kaon decay

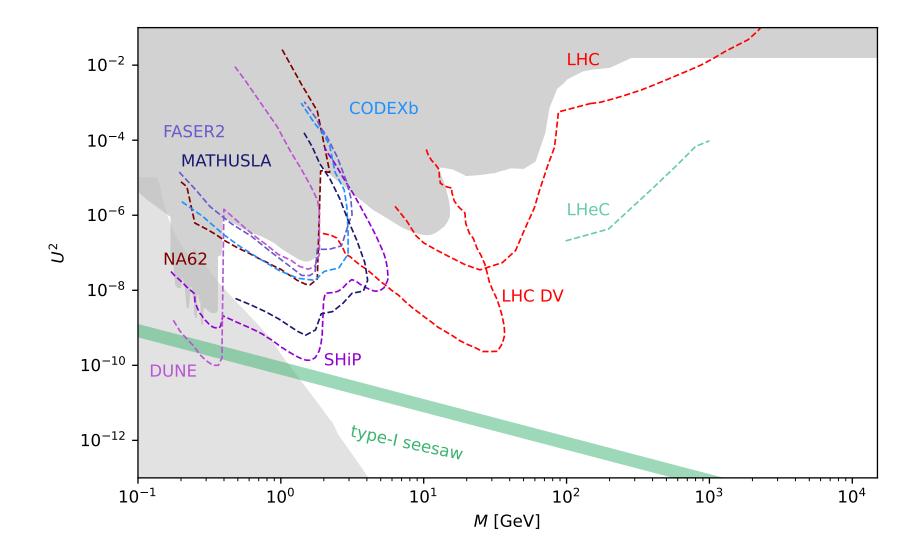
LHC: Off-shell W/Z decay

Upgraded Bounds



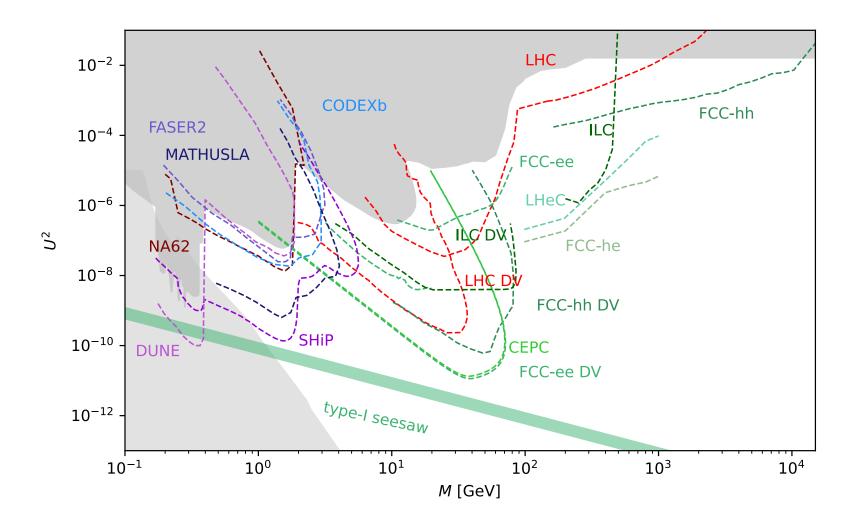
Future Upgraded Projection on LHC, NA62 and DUNE

Various Bounds



Some future proposed beam-dump experiments or far detector to probe the long-lived HNL

Various Bounds



Bounds from the proposed future collider: FCC, CEPC, ILC, LHeC

Conclusion

- Muon Collider is a good platform to probe the TeV scale HNL.
 We can open a new region in the parameter space.
- For the muon flavor case, we can probe the Umu^2 down to 10^(-6) for mN larger than O(100) GeV.
- There are t-channel singularity cases one should be careful to deal with.